# **CONTRAST ENHANCEMENT**

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First Semester 2016/2017

### Outline

- What is Image Enhancement ?
- Background
- Intensity Transformation Functions
  - Negatives
  - Log and Inverse Log
  - Power-Law
  - Piecewise Transformation
  - Gray-level and Bit Slicing
- Histogram Processing
  - Equalization
  - Specification
  - Local Processing

## What is a Digital Image? (cont...)

- 3
- Spatial domain of the image is the set of pixels composing the image
- Enhancement in the spatial domain involves direct operation on the pixel intensities
- This can be expressed mathematically as

### g(x,y) = T[f(x,y)]

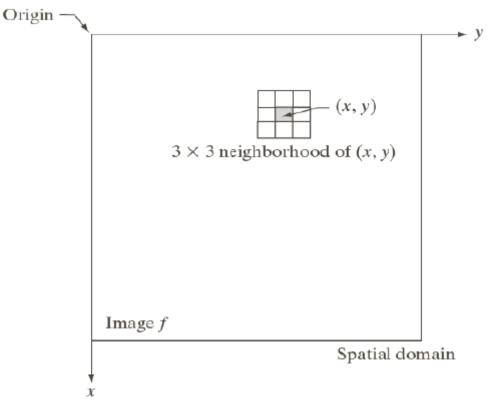
- f(x,y) is the input image
- g(x,y) is the output image
- T[] is an operator defined over some neighborhood of (x,y)

### Important

Keep in mind that g(x,y) may take any value from the set of available gray levels only. Thus, when mapping we should assign the mapped value to the closest level

## What is a Digital Image? (cont...)

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- Defining the neighborhood around (x,y)
  - Use a square/rectangular subimage that is centered at (x,y)
- Operation
  - Move the center of the subimage from pixel to pixel and apply the operator T at each location (x,y) to compute the output g(x,y)



### **Point Processing**

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- The simplest form of the operator T is when the neighborhood size is 1x1 pixels. Accordingly, g(x,y) is only dependent on the value of f at (x,y)
- In this case, T is called the gray-level or intensity transformation function that can be represented as

# s = T(r)

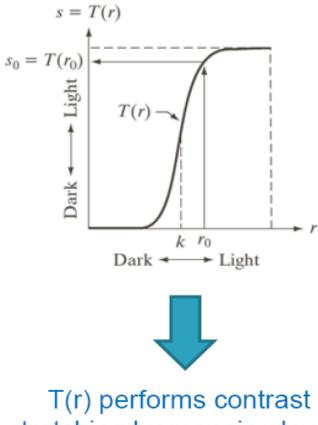
- s is a variable denoting g(x,y)
- r is a variable denoting f(x,y)

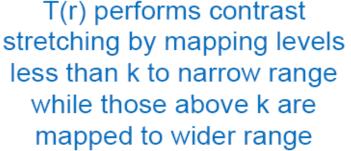
This is kind of processing is referred as point processing

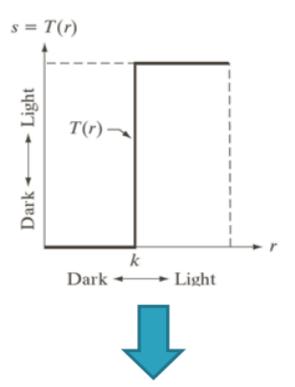
### **Point Processing - Example**

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### Intensity transformation function examples



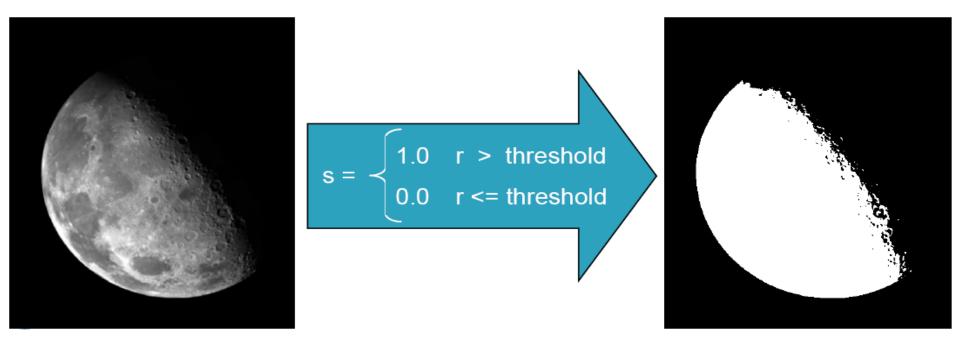




T(r) reduces the number of levels in the image to two

## **Point Processing Example - Thresholding**

Thresholding transformations are particularly useful for segmentation in which we want to isolate an object of interest from a background

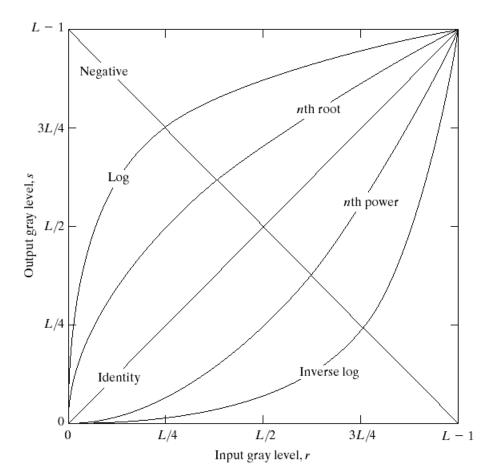


### Image enhancement: Contrast Enhancement

- Contrast is an important factor in any subjective evaluation of image quality.
- Contrast is created by the difference in luminance reflected from two adjacent surfaces. In other words, contrast is the difference in visual properties that makes an object distinguishable from other objects and the background.
- In visual perception, contrast is determined by the difference in the colour and brightness of the object with other objects.
- Contrast enhancements are typically performed as a contrast stretch followed by a tonal enhancement, although these could both be performed in one step.

### **Contrast Enhancement - Gray Level** Transformations

- Contrast Enhancement done by pixel value mapping called Gray Level Transformations
- Mapping can be performed by mathematical substitution or lookup tables
- Some common functions are
  - Linear (negative/identity)
  - Logarithmic (log/inverse log)
  - Power law (nth power/nth root)
  - Piecewise-Linear Transformations



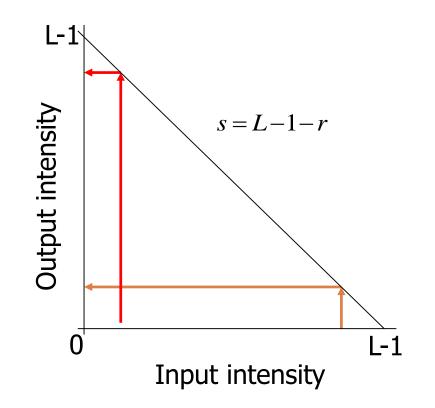
### **Image Negatives**

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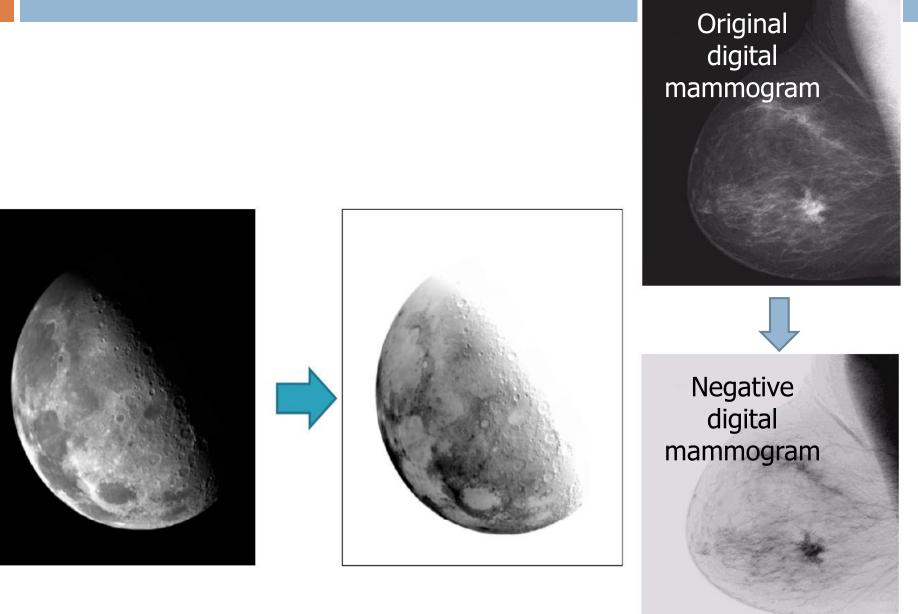
Can be performed by using

s = L - 1 - r

where L-1 is the maximum intensity value



### Image Negatives - Example



### Log and inverse Log Transformations

The general form of the log transformation

 $s = clog_b(1+r)$ 

b is the base

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- Maps narrow range of low intensity levels to wider range and wide range of high intensity levels to narrower range
- Usually used to expand the values of dark pixels and compress the higher level values

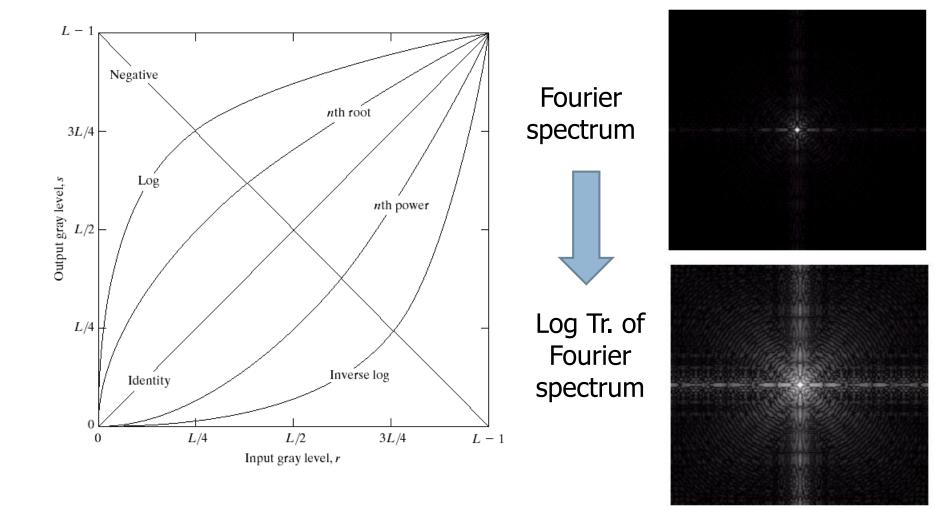
The general form of the inverse log

$$s = b^{cr} - 1$$

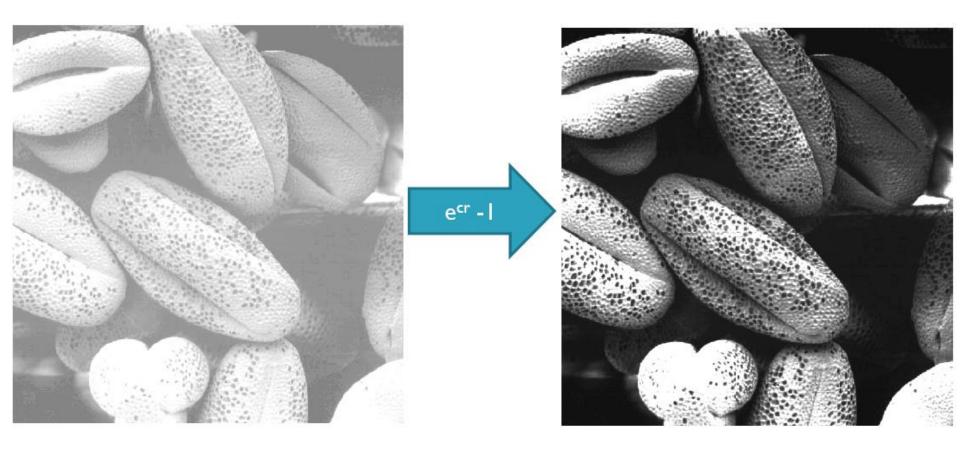
Its operation is the opposite of the log transformation

## Log Transformation Example

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- It is very important in mapping wide dynamic ranges into narrow ones
- Fourier spectrum values in the range [0,1.5x10<sup>6</sup>] transformed to [0,255] using log transformation



### Inverse Log Transformation Example



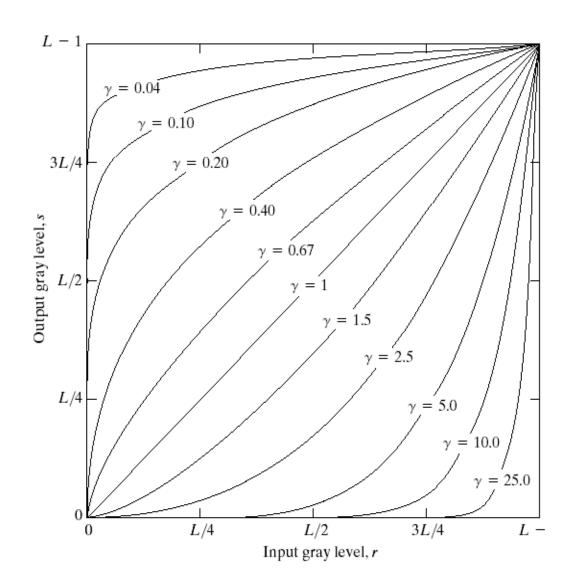
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The general form

 $s = cr^{\gamma}$ 

- Power law is similar to log when gamma < 1 and similar to inverse log when gamma > 1
- Like the logarithmic transform, they are used to change the dynamic range of an image. However, in contrast to the logarithmic operator, they enhance high intensity pixel values.

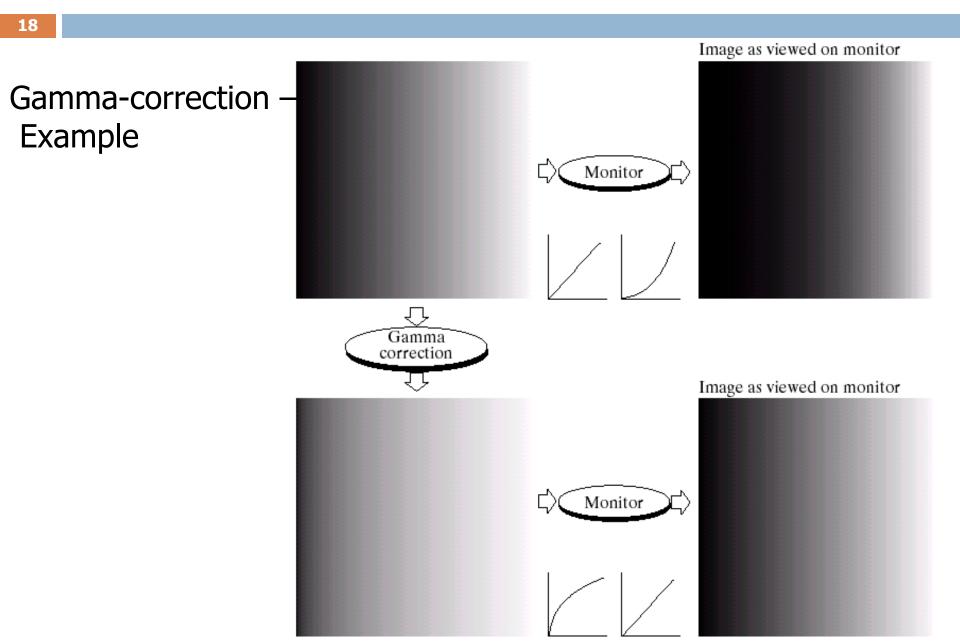
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power-law curves with fractional values of <sup>y</sup> map a narrow range of dark input values to a wider range of output values, and opposite for higher values of input levels

### Gamma-correction

- Display devices have intensity-to-voltage response that is a power functions. Thus, images tend to be darker when displayed. Correction is needed using nth root before feeding the image to the monitor
- Solution –display image after gamma correction to value that represents "average" of the types of monitors and computer systems to be used to display the image.



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 Gammacorrection application



#### a b c d

#### FIGURE 3.8

(a) Magnetic resonance (MR) image of a fractured human spine. (b)-(d) Results of applying the transformation in Eq. (3.2-3) with c = 1 and  $\gamma = 0.6, 0.4, and$ 0.3, respectively. (Original image for this example courtesy of Dr. David Ř. Pickens, Department of Radiology and Radiological Sciences, Vanderbilt University Medical Center.)

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### Gammacorrection application

a b c d FIGURE 3.9 (a) Aerial image. (b)–(d) Results of applying the transformation in Eq. (3.2-3) with c = 1 and  $\gamma = 3.0, 4.0, \text{ and}$ 5.0, respectively. (Original image for this example courtesy of

NASA.)



### **Piecewise-Linear Transformations**

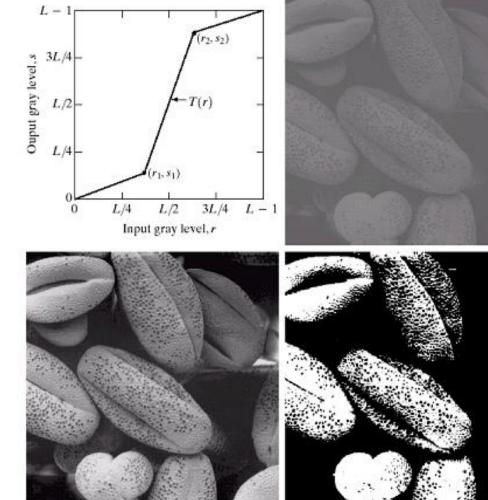
- 21
- Can represent arbitrarily complex functions to achieve different results
  - Contrast stretching
  - Gray-level Slicing
  - Bit-plane Slicing

## **Contrast Stretching**

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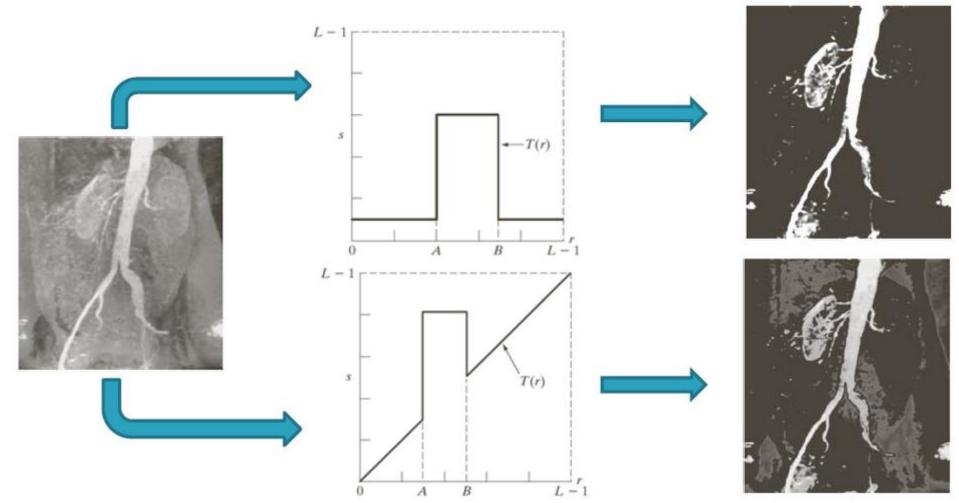
Improve the contrast by `stretching' the range of intensity values it contains to span a desired range of values

- r1 ≤ r2 and s1 ≤ s2 to preserve the order of gray levels
- The result depends on the values of r1, r2, s1, and s2



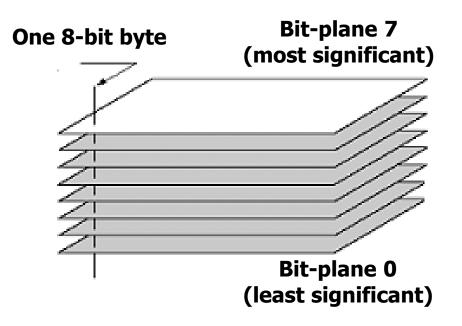
## **Gray-level Slicing**

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- Used to highlight specific range of gray levels
- Two approaches

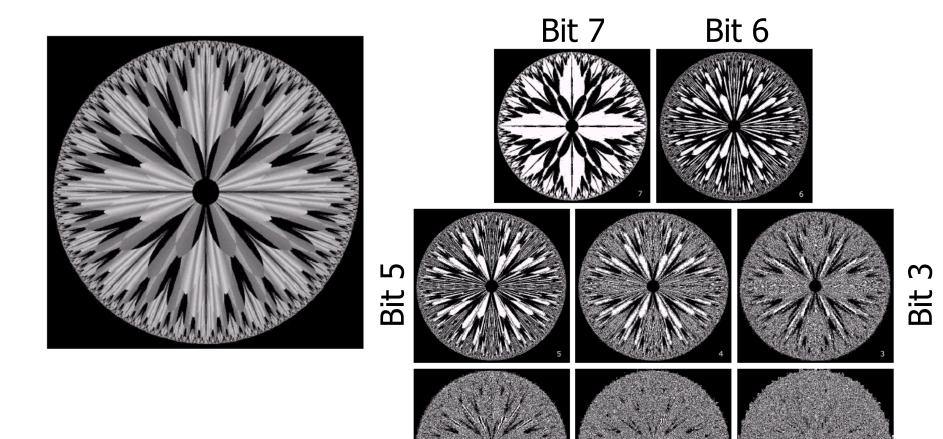


## **Bit-plane Slicing**

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- Highlight the contribution of specific bits to the appearance of the image
- Each pixel value is represented by a set of bits
- Lower bits correspond to fine details while higher bits correspond to the global visual content
- Useful in image compression !

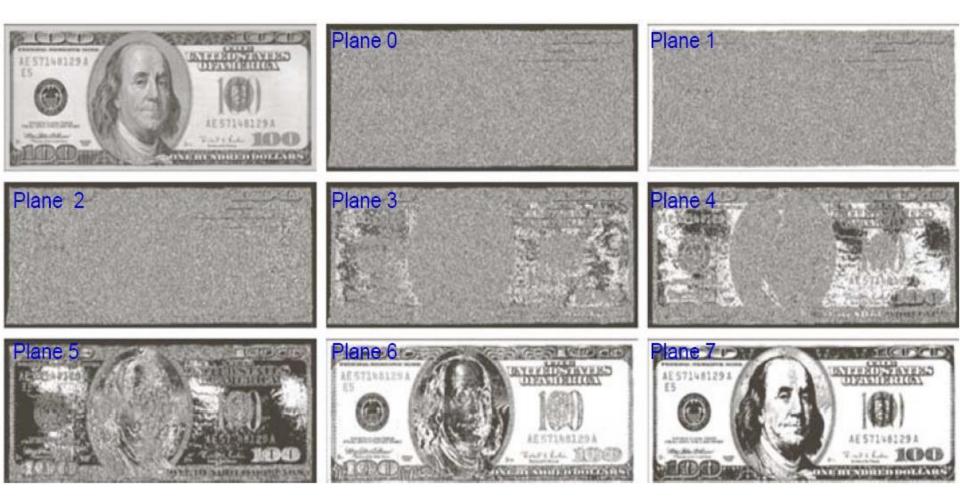


### **Bit-plane Slicing - example**



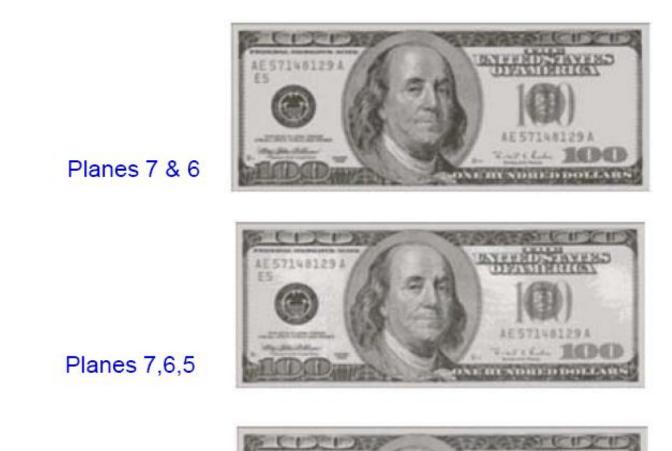
Bit 2 Bit 1

### **Bit-plane Slicing - example**



### **Bit-plane Slicing - example**

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AE571+8129A

AE57148129A

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Planes 7,6,5,4

## Histogram Processing

For an image with gray levels in [0,L-1] and MxN pixels, the histogram is a discrete function given by



Where

- *r<sub>k</sub>*: the k<sup>th</sup> gray level
- **n\_k**: the number of pixels in the image having gray level  $r_k$
- $h(r_k)$ : histogram of a digital image with gray levels  $r_k$
- It is a common practice to normalize the histogram function by the number of pixels in the image by

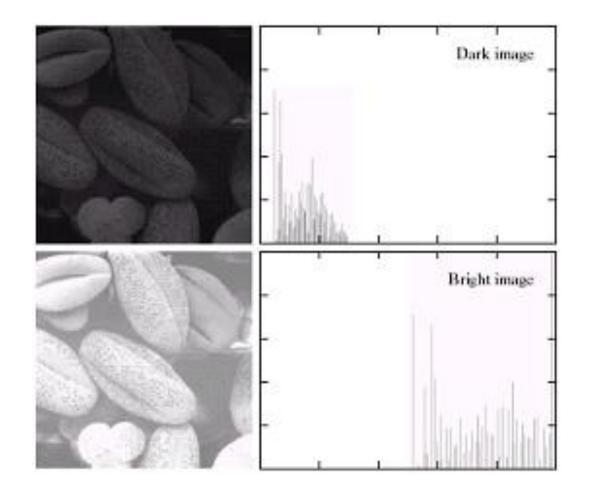
$$p(r_k) = n_k / n$$

- The normalized histogram can be used as an estimate of the probability density function of the image
- Histograms are widely used in image processing: enhancement, compression, segmentation ...

## **Histogram Processing**

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For enhancement, histograms can be used to infer the type of image quality: dark, bright, low or high contrast



### Dark image

Components of histogram are concentrated on the low side of the gray scale.

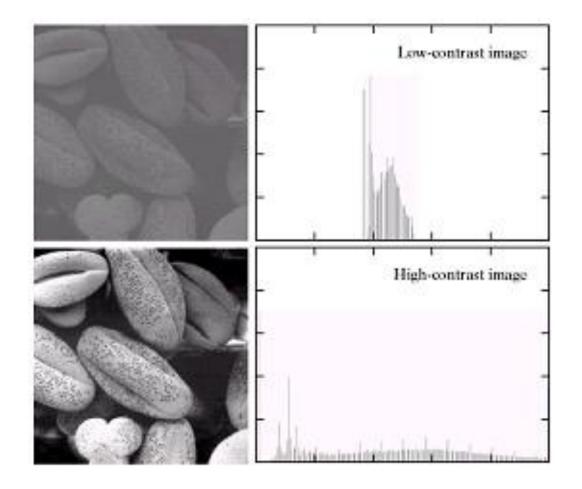
### Bright image

Components of histogram are concentrated on the high side of the gray scale.

## **Histogram Processing**

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For enhancement, histograms can be used to infer the type of image quality: dark, bright, low or high contrast



### Low-contrast image

histogram is narrow and centered toward the middle of the gray scale

### High-contrast image

histogram covers broad range of the gray scale and the distribution of pixels is not too far from uniform, with very few vertical lines being much higher than the others

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- It is quite acceptable that high contrast images have flat histograms (uniform distribution)
- As the low-contrast image's histogram is narrow and centered toward the middle of the gray scale, if we distribute the histogram to a wider range the quality of the image will be improved.
- We can do it by adjusting the probability density function of the original histogram of the image so that the probability spread equally
- Histogram equalization attempts to transform the original histogram into a flat one for the goal of better contrast

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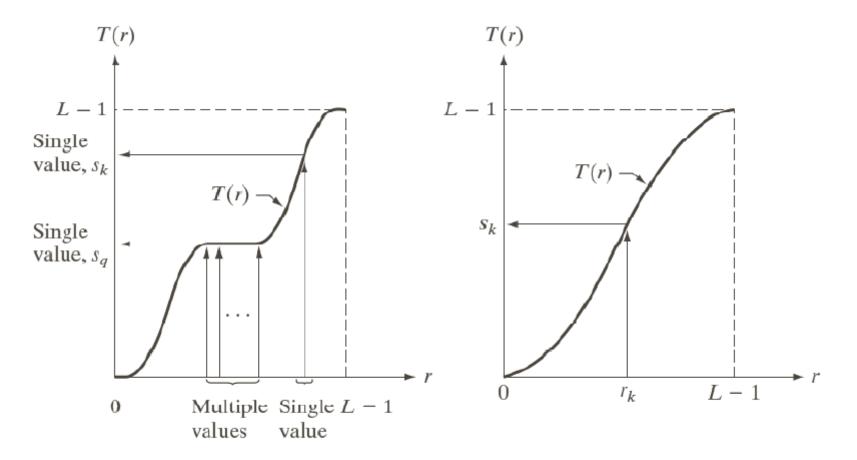
- Let r be a continuous variable that represents the intensity values in the range [0,L-1], then a valid transformation function for enhancement purposes s = T(r) should satisfy
  - **T**(r) is monotonically increasing in the interval  $0 \le r \le L-1$ 
    - Preserves the increasing order from black to white in the output image thus it won't cause a negative image
  - T(r) is bounded by [0,L-1] for all values of r
    - Guarantees that the output gray levels will be in the same range as the input levels.
  - The inverse transformation function that maps s back to r

$$r=T^{-1}(s)$$

requires that T(r) to be strictly monotonically increasing

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### Examples of transformation functions



### Monotonically Increasing

### Strictly monotonically increasing

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- Consider the gray level intensity represented by r as a random variable in the interval [0,L-1]
- If a random variable *r* is transformed by a monotonic transformation function *T(r)* to produce a new random variable *s*,
- Then probability density function of s can be obtained from knowledge of T(r) and the probability density function of s, as follows:

$$p_s(s) = p_r(r) \left| \frac{dr}{ds} \right|$$

Note that the probability density function (pdf or shortly called density function) of random variable x is defined as the derivative of the cdf

$$p(x) = \frac{dF(x)}{dx}$$

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A transformation function of a particular importance in image processing has the form:

$$s = T(r) = (L-1) \int_{0}^{r} p_{r}(w) dw$$

- Where w is a dummy variable of integration
- CDF is an integral of a probability function (always positive) is the area under the function. Thus, CDF is always single valued and monotonically increasing. Thus, CDF satisfies the condition (a)
- When the upper limit is r = L-1 the integral evaluates to 1. thus condition (b) satisfied also.

$$\frac{ds}{dr} = \frac{dT(r)}{dr}$$

$$= (L-1)\frac{d}{dr} \left[ \int_{0}^{r} p_{r}(w) dw \right]$$

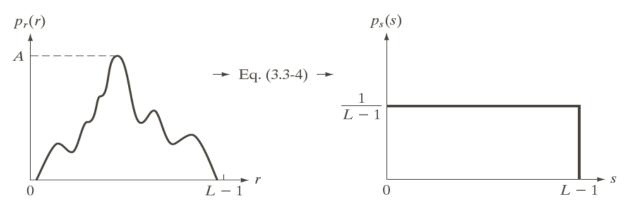
$$= (L-1)p_{r}(r)$$

$$p_{s}(s) = p_{r}(r) \left| \frac{dr}{ds} \right|$$

$$= p_{r}(r) \left| \frac{1}{(L-1)p_{r}(r)} \right|$$
Substitute and yield
$$= \frac{1}{L-1} \text{ where } 0 \le s \le 1$$

$$s = T(r) = \int_{0}^{r} p_{r}(w) dw$$

#### a random variable s yields characterized by a uniform probability function



a b

**FIGURE 3.18** (a) An arbitrary PDF. (b) Result of applying the transformation in Eq. (3.3-4) to all intensity levels, *r*. The resulting intensities, *s*, have a uniform PDF, independently of the form of the PDF of the *r*'s.

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The probability of occurrence of gray level in an image is approximated by

$$p_r(r_k) = \frac{n_k}{n}$$
 where  $k = 0, 1, ..., L-1$ 

The discrete version of transformation

$$s_{k} = T(r_{k}) = (L-1) \sum_{j=0}^{k} p_{r}(r_{j})$$
$$= (L-1) \sum_{j=0}^{k} \frac{n_{j}}{n} \quad where \ k = 0, 1, ..., L-1$$

Thus, an output image is obtained by mapping each pixel with level  $r_k$  in the input image into a corresponding pixel with level  $s_k$  in the output image

•	[ • ]	
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r <sub>k</sub>	$n_k$	$p_r(r_k) = n_k/MN$	TABLE 3.1     Intensity	s <sub>k</sub>	Valu e	Appr	Ps(s)
$r_0 = 0$ $r_1 = 1$	790 1023	0.19 0.25	distribution and histogram values for a 3-bit,	s 0	1.33	1	
$r_2 = 2$ $r_3 = 3$ $r_4 = 4$	850 656 329	0.21 0.16 0.08	$64 \times 64$ digital image.	s 1	3.08	3	790/4096
$r_5 = 5$ $r_6 = 6$	245 122	0.06 0.03		s 2	4.55	5	
$r_7 = 7$	81	0.02		s 3	5.67	6	1023/4096
$p_r(r_k)$		s <sub>k</sub>	$p_s(s_k)$	s 4	6.23	6	
.2520 -		7.0	.25 + .20 +	s 5	6.65	7	$s_k = T(r_k)$
.15 + .10 + .05 +	•	4.2 + 2.8 + T(r) 1.4 + T(r)	.15 + .10 + .05 +	s 6	6.86	7	$= (L-1)\sum_{j=0}^{k} \frac{n_j}{n}$
0 1 2 3	4 5 6 7	$r_k$	$r_k$	s 7	7.00	7	(245+122+81)/4096

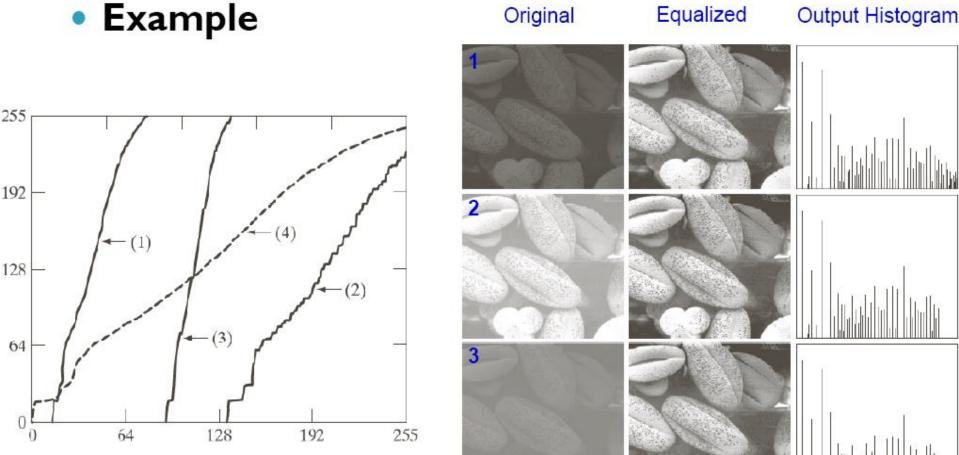
#### a b c

**FIGURE 3.19** Illustration of histogram equalization of a 3-bit (8 intensity levels) image. (a) Original histogram. (b) Transformation function. (c) Equalized histogram.

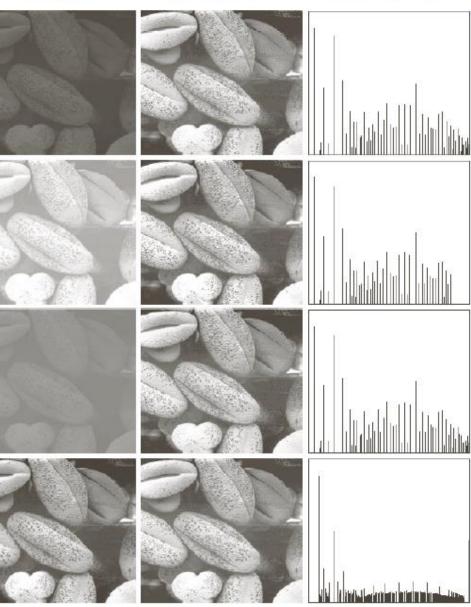
### It is clearly seen that

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- Histogram equalization distributes the gray level to reach the maximum gray level (white) because the cumulative distribution function equals 1 when 0 ≤ r ≤ L-1
- If the cumulative numbers of gray levels are slightly different, they will be mapped to little different or same gray levels as we may have to approximate the processed gray level of the output image to integer number
- Thus the discrete transformation function can't guarantee the one to one mapping relationship



Transformation for the processed images

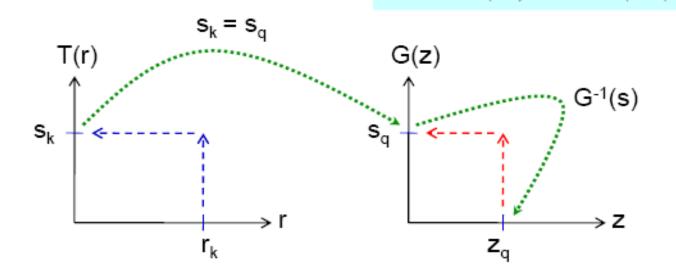


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- Histogram equalization has a disadvantage which is that it can generate only one type of output image.
- With Histogram Specification, we can specify the shape of the histogram that we wish the output image to have.
- We can use the method used in deriving the transformation function of histogram equalization to find transformation function for the desired histogram, however
  - This requires the availability of p<sub>s</sub>(s) in mathematical form and the ability to express s in terms of r
  - It doesn't have to be a uniform histogram
  - Histogram specification is a trial-and-error process
  - There are no rules for specifying histograms, and one must resort to analysis on a case-by-case basis for any given enhancement task.

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#### Alternatively

 Let p<sub>r</sub>(r) and p<sub>z</sub>(z) denote the original and desired histograms and assume that there exist two transformation functions s = T(r) and s = G(z). This implies that we can find the mapping from r to s by knowing the inverse of G(z) z = G<sup>-1</sup>(s) = G<sup>-1</sup>(T(r))



This is a simple operation if G<sup>-1</sup>(s) can be obtained !!!!

### The algorithm

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1. Obtain the transformation function T(r) by calculating the histogram equalization of the input image

$$s = T(r) = \int_{0}^{r} p_{r}(w) dw$$

2. Obtain the transformation function G(z) by calculating histogram equalization of the desired density function

$$G(z) = \int_{0}^{z} p_{z}(t) dt = s$$

### The algorithm

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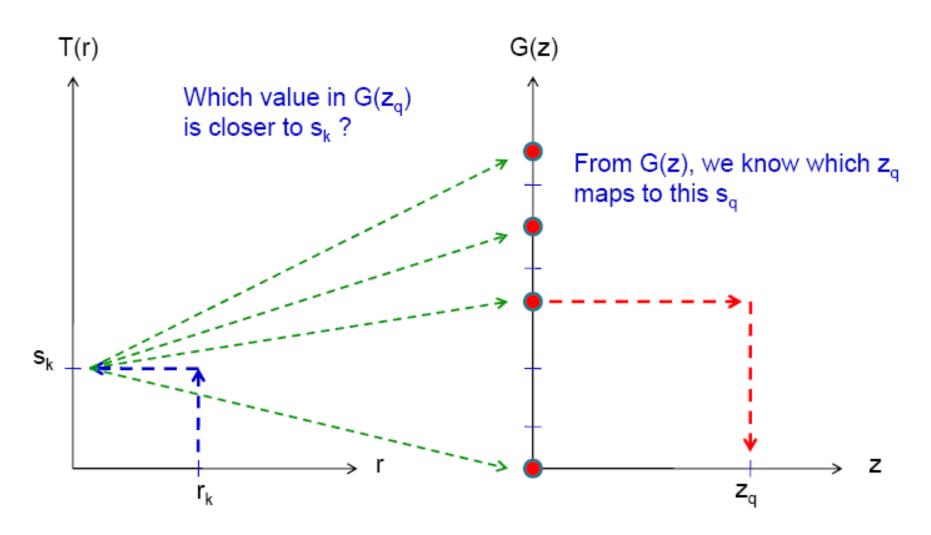
3. Obtain the inversed transformation function G<sup>-1</sup> (mapping from s to z)

$$z = G^{-1}(s) = G^{-1}[T(r)]$$

4. Obtain the output image by applying the processed gray-level from the inversed transformation function to all the pixels in the input image

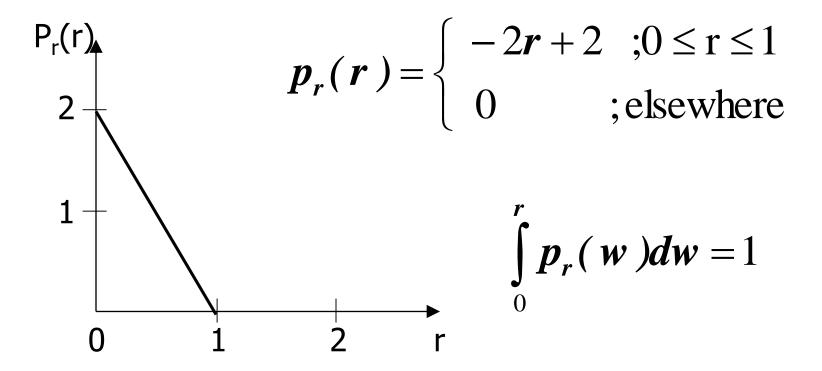
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Illustration



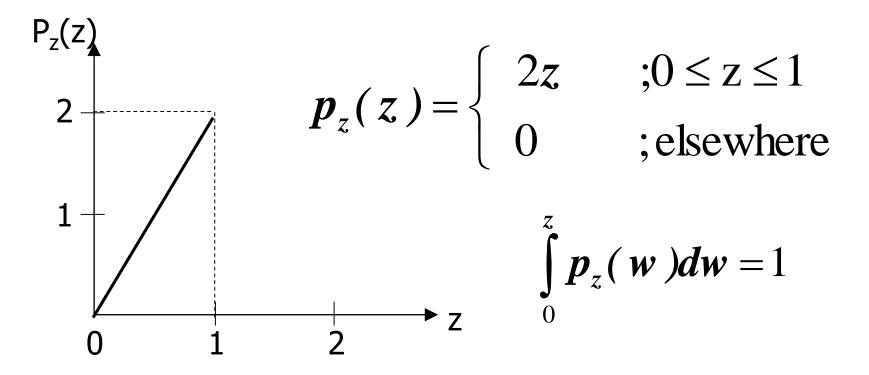


Assume an image has a gray level probability density function  $p_r(r)$  as shown.



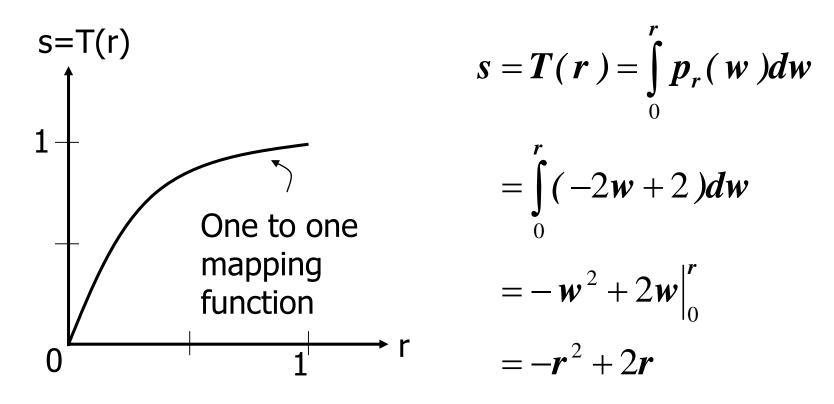
### Example

We would like to apply the histogram specification with the desired probability density function  $p_z(z)$  as shown.



### Step 1:

### Obtain the transformation function T(r)





### Obtain the transformation function G(z)

$$G(z) = \int_{0}^{z} (2w) dw = z^{2} \Big|_{0}^{z} = z^{2}$$



### Obtain the inversed transformation function $G^{-1}$

$$G(z) = T(r)$$
$$z^{2} = -r^{2} + 2r$$
$$z = \sqrt{2r - r^{2}}$$

We can guarantee that  $0 \leq z \leq 1$  when  $0 \leq r \leq 1$ 

### **Discrete formulation**

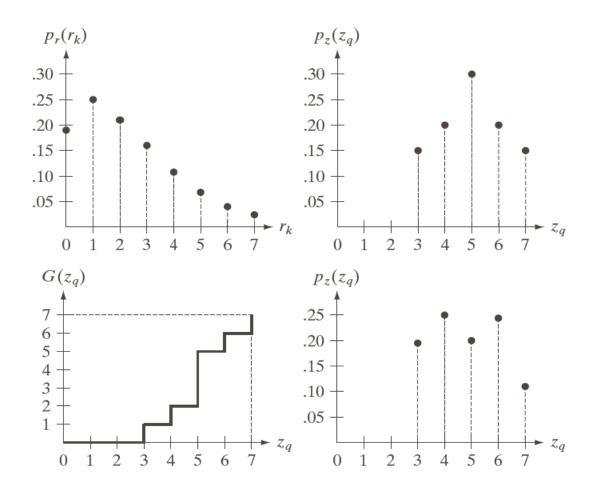
J

$$s_{k} = T(r_{k}) = (L-1) \sum_{j=0}^{k} p_{r}(r_{j})$$
$$= (L-1) \sum_{j=0}^{k} \frac{n_{j}}{n} \qquad k = 0, 1, 2, \dots, L-1$$

$$G(z_k) = (L-1)\sum_{i=0}^k p_z(z_i) = s_k \qquad k = 0, 1, 2, \dots, L-1$$

$$z_{k} = G^{-1}[T(r_{k})]$$
  
=  $G^{-1}[s_{k}]$   $k = 0, 1, 2, ..., L-1$ 

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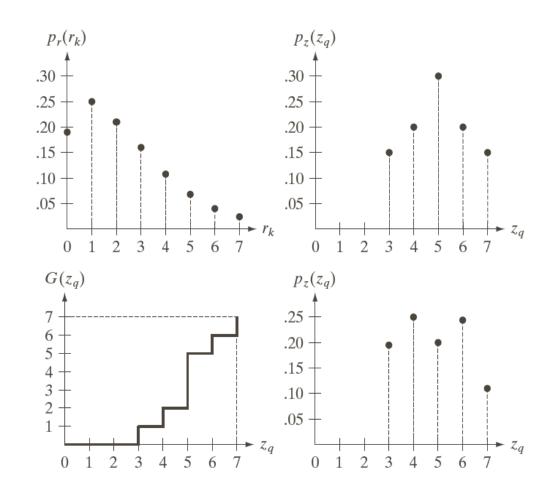


a b c d

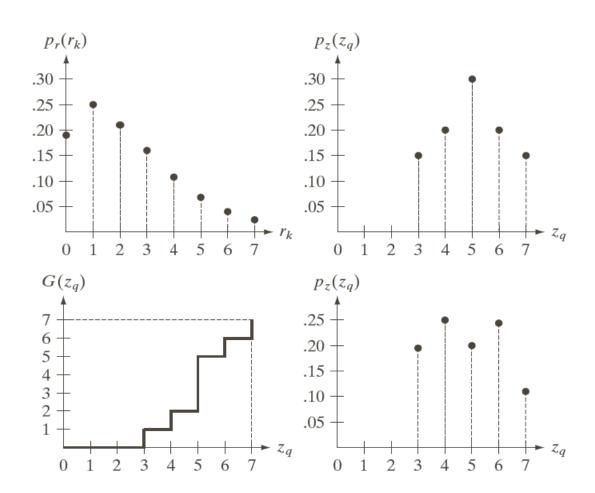
#### FIGURE 3.22

(a) Histogram of a
3-bit image. (b)
Specified
histogram.
(c) Transformation
function obtained
from the specified
histogram.
(d) Result of
performing
histogram
specification.
Compare
(b) and (d).

r <sub>k</sub>	$n_k$	$p_r(r_k) = n_k/MN$
$r_0 = 0$	790	0.19
$r_1 = 1$	1023	0.25
$r_2 = 2$	850	0.21
$r_3 = 3$	656	0.16
$r_4 = 4$	329	0.08
$r_5 = 5$	245	0.06
$r_6 = 6$	122	0.03
$r_7 = 7$	81	0.02

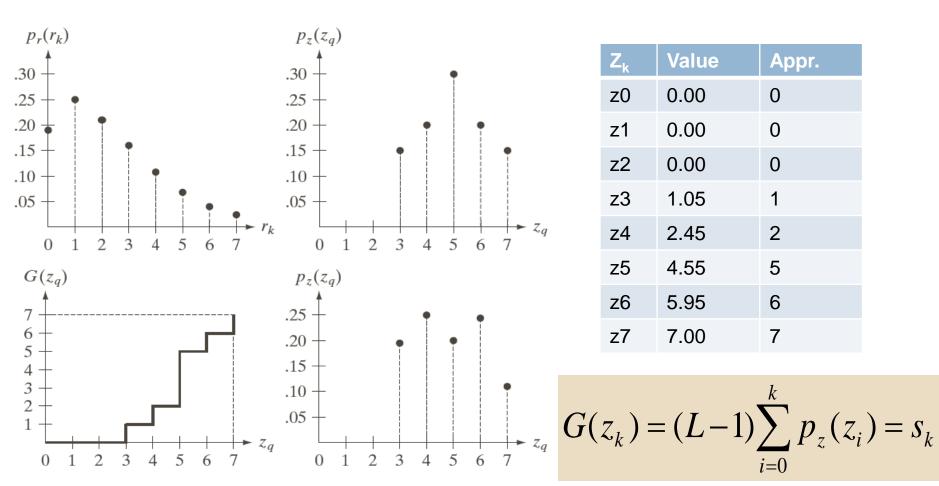


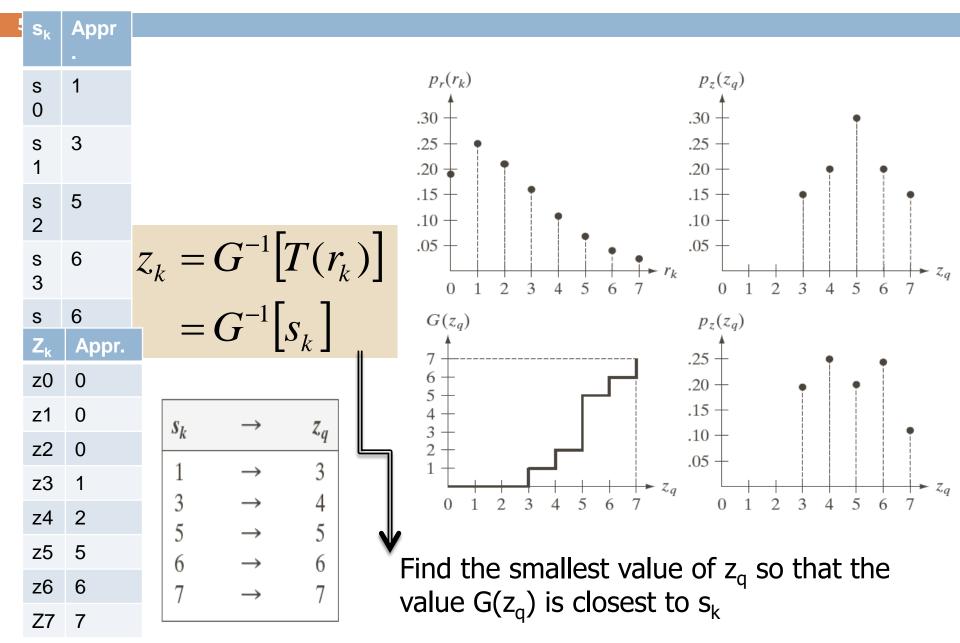
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Zq	Specified Pz(Zq)
z0	0.00
z1	0.00
z2	0.00
z3	0.15
z4	0.20
z5	0.30
z6	0.20
z7	0.15

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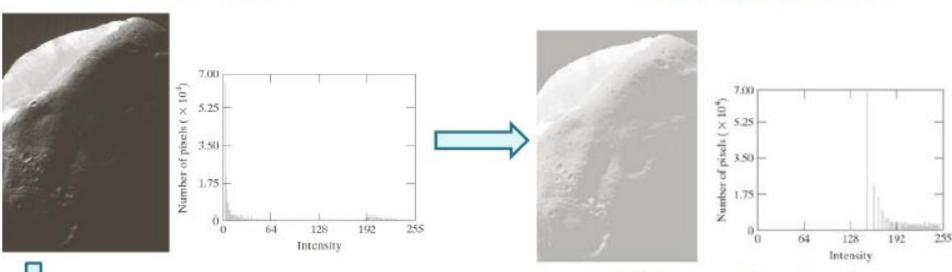


<b>Histogram Specification</b>	r <sub>k</sub>	Nk	s <sub>k</sub>	Appr			
	r0	790	c	1			
58	r1	1023	s 0	'			
$\mathbf{p}(\mathbf{r})$	r2	850	S	3	<i>s</i> <sub>k</sub>	$\rightarrow$	$Z_q$
$p_r(r_k)$ $p_z(z_q)$	r3	656	1	0	1	$\rightarrow$	3
.30 +	r4	329	s	5	35	$\rightarrow$	4
$.20$ $\bullet$ $.20$ $\bullet$ $\bullet$ $\bullet$	r5	245	2		6	$\rightarrow$ $\rightarrow$	5
.1515 -	r6	122	s 3	6	7	$\rightarrow$	7
.10 +10 +05 +	r7	81	S	6			
	Zq	Speci	4	Ŭ			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		d Pz(Zq	s 5	7			
	z0		S	7			
$\begin{array}{c} 0 \\ 5 \\ 4 \end{array}$	z1	0.00	6				
310 -	z2	0.00	s 7	7			
	z3	0.15		790/40	96=0.1	9	
0 1 2 3 4 5 6 7 0 1 2 3 4 5 6 7	z4	0.20		1023/4	096=0.2	25	
	z5	0.30		850/40	96=0.2 <sup>-</sup>	1	
	z6	0.20		(656+3	29)/409	96=0.24	ŀ
	z7	0.15		(245+1	22+81)	/4096=	0.11

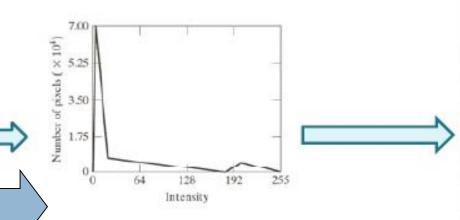
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#### **Original Image**

#### Histogram Equalization

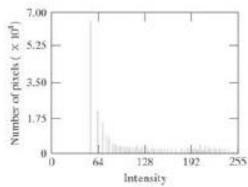


#### **Desired Histogram**



#### **Histogram Specification**

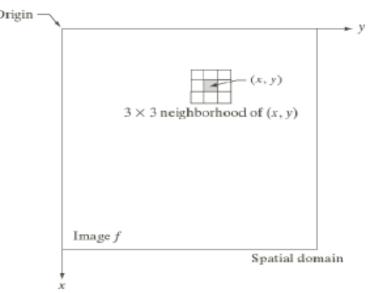




### **Local Histogram Processing**

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- Both histogram equalization and specification methods discussed earlier are considered global
- In other words, pixels are modified using a transformation function that is defined using all pixels in the image
- Such methods are suitable for overall enhancement and may not be suitable in situations where we want to enhance small areas in the image whose pixel count contributes less to the global transformation function

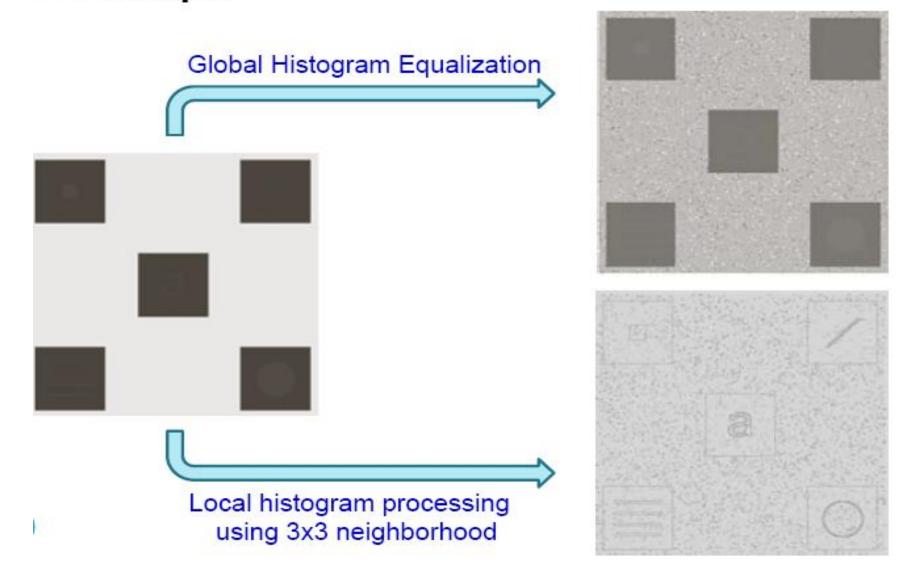
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- Solution: Consider local processing such that for each pixel (x,y) in the image
  - Define a small neighborhood of size mxn that is centered around the pixel
  - Use pixels inside the neighborhood to construct the transformation function
  - Use the computed function map the pixel at (x,y)
  - Repeat for all pixels



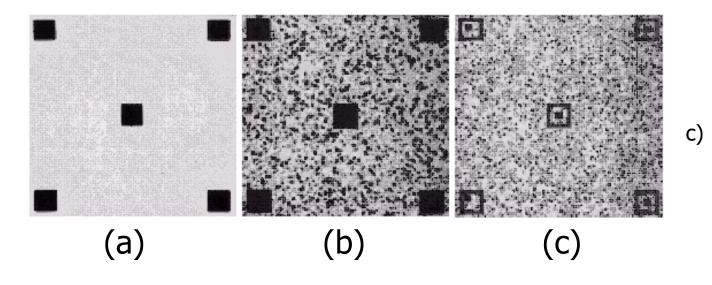
### **Local Histogram Processing**

• Example

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### Local Enhancement



- a) Original image (slightly blurred to reduce noise)
- b) global histogram equalization (enhance noise & slightly increase contrast but the construction is not changed)
  - local histogram equalization using 7x7 neighborhood (reveals the small squares inside larger ones of the original image.
- define a square or rectangular neighborhood and move the center of this area from pixel to pixel.
- at each location, the histogram of the points in the neighborhood is computed and either histogram equalization or histogram specification transformation function is obtained.
- another approach used to reduce computation is to utilize nonoverlapping regions, but it usually produces an undesirable checkerboard effect.

### Explain the result in c

- Basically, the original image consists of many small squares inside the larger dark ones.
- However, the small squares were too close in gray level to the larger ones, and their sizes were too small to influence global histogram equalization significantly.
- So, when we use the local enhancement technique, it reveals the small areas.
- Note also the finer noise texture is resulted by the local processing using relatively small neighborhoods.